Designing and Drawing a Sprocket

Visualizing ideas through the creation of CAD solid models is a key engineering skill.

The following text offers the information and procedural steps necessary to engineer a CAD profile of the #25 pitch, 30 tooth sprocket found in the GEARS-IDS™ kit of parts.

This process provides a method for generating solid models of any standard sprocket, pitch, number of teeth, or configuration. This exercise also provides students and instructors with an excellent way to incorporate 8th and 9th grade algebra and geometry knowledge with engineering drawing skills to produce the design elements necessary to fully visualize their mechanical creations.

Fig. 1 Sprocket Tooth Geometry
(Adapted from the American Chain Association Chains for Power Transmission and Material Handling handbook.)
Sprocket Tooth Design Formulas
Refer to Fig. 1 Sprocket Tooth Geometry

The tooth form of a sprocket is derived from the geometric path described by the chain roller as it moves through the pitch line, and pitch circle for a given sprocket and chain pitch. The shape of the tooth form is mathematically related to the Chain Pitch \( P \), the Number of Teeth on the Sprocket \( N \), and the Diameter of the Roller \( D_r \). The formulas for the seating curve, radius \( R \) and the topping curve radius \( F \) include the clearances necessary to allow smooth engagement between the chain rollers and sprocket teeth.

The following formulas are taken from the American Chain Association Chains for Power Transmission and Material Handling handbook, and they represent the industry standards for the development of sprocket tooth forms.

\[
\begin{align*}
P & = \text{Chain Pitch} \\
N & = \text{Number of Teeth} \\
D_r & = \text{Roller Diameter (See Table)} \\
Ds & = \text{(Seating curve diameter)} = 1.0005 \ D_r + 0.003 \\
R & = \frac{Ds}{2} = 0.5025 \ D_r + 0.0015 \\
A & = 35^\circ + \frac{60^\circ}{N} \\
B & = 18^\circ - \frac{56^\circ}{N} \\
ac & = 0.8 \times D_r \\
M & = 0.8 \times D_r \cos(35^\circ + \frac{60^\circ}{N}) \\
T & = 0.8 \times D_r \sin \left(35^\circ + \frac{60^\circ}{N}\right) \\
E & = 1.3025 \ D_r + 0.0015 \\
\text{Chordal Length of Arc}\ xy & = (2.605 \ D_r + 0.003) \sin \left(9^\circ - \frac{28^\circ}{N}\right)
\end{align*}
\]

\[
\begin{align*}
yz & = Dr \left[1.4 \sin(17^\circ - \frac{64^\circ}{N}) - 0.8 \sin(18^\circ - \frac{56^\circ}{N})\right] \\
ab & = 1.4 \ D_r \\
W & = 1.4 \ D_r \cos \frac{180^\circ}{N} \\
V & = 1.4 \ D_r \sin \frac{180^\circ}{N} \\
F & = D_r \left[0.8 \cos(18^\circ - \frac{56^\circ}{N}) + 1.4 \cos(17^\circ - \frac{64^\circ}{N}) - 1.3025\right] - 0.0015 \\
H & = \sqrt{F^2 - \left(1.4D_r - \frac{P}{2}\right)^2} \\
S & = \frac{P}{2} \cos \frac{180^\circ}{N} + H \sin \frac{180^\circ}{N} \\
PD & = \frac{P}{\sin \frac{180^\circ}{N}}
\end{align*}
\]

Table 1
Procedure for Drawing a Sprocket

In this example we will draw the tooth form for the GEARS-IDS 30 tooth Sprocket. Refer to Fig.1, the Sprocket Formulas and the Maximum Roller Diameter Table.

NOTE: This is primarily an algebra and geometry exercise. When drawing a sprocket model for the first time there will likely be problems with arcs that are not exactly tangent to lines, or line lengths that are not exact to 3 or 4 decimal places. This can cause problems if you are using modeling software. Use your drawing tools and common sense in order to create tangent relationships and working line lengths.

With experience, it is possible to draw extremely accurate sprocket models by using the associated spreadsheet and following the directions below.

<table>
<thead>
<tr>
<th>Chain Number</th>
<th>Pitch</th>
<th>Max Roller Diameter</th>
</tr>
</thead>
<tbody>
<tr>
<td>25</td>
<td>¼&quot;</td>
<td>0.130*</td>
</tr>
<tr>
<td>35</td>
<td>3/8</td>
<td>0.200*</td>
</tr>
<tr>
<td>41</td>
<td>½&quot;</td>
<td>0.306</td>
</tr>
<tr>
<td>40</td>
<td>½&quot;</td>
<td>5/16</td>
</tr>
</tbody>
</table>

* This refers to the bushing diameter since the chain pitch is small and roller-less.

1.) Determine the values for P, N and Dr for a 30T sprocket

2.) Calculate the remaining values using the formulas on the preceding page.

Enter the data in the table below.

Note: this can be accomplished with a calculator or by using the GEARS-IDS™ spreadsheet (sprocketequations.xls)
3.) Draw the Pitch Circle using a radius equal to \( \frac{1}{2} \) PD. (Radius = 1.19585 for this example)

Note: In order to obtain the best results, it will be necessary to fully constrain all the entities. Often it is helpful to fix the entities or geometry as they are created. Specify dimension values to 4 decimal places.

4.) Draw a construction line (1, 2) from the center of the circle through the top quadrant. Where this line intersects the circle is the location of point a.

5.) Draw a horizontal line (3, 4) through point a, (the top quadrant,) of the pitch circle. Make this line tangent to the pitch circle.

6.) Draw a circle with radius = \( R \) at the intersection of lines 1,2 and 3,4.

Radius = \( R \) from calculations or spreadsheet = 0.0668”
7.) Offset lines 1,2 and 3,4 distances M and T respectively. These lines will intersect at point c

Note: Throughout this exercise it is important to continually save your work and to continually verify the accuracy of every dimension.

8.) Draw line cx at angle A. Line cx must extend beyond the circle.

9.) Draw line cy. Line cy = length E (E = .1708 for this example) and is drawn at an angle B from cx.
10.) Draw arc xy (Shown in blue) with radius E. 
(E = .1708 for this example)

Use the 3 point arc command to set the arc from point x to point y. After drawing the arc dimension the radius to length E)

Note: The center of arc xy appears to be at or near point c. Do not make the assumption that this is always the case. With sprockets of differing numbers of teeth, the center of arc xy will likely NOT be at point c.

The image on the right illustrates the arc dimension for the 30 tooth #25 pitch sprocket used in this example.
11.) Draw line segment $yz$ (Shown in green) perpendicular to line $cy$. This can be drawn initially to any point on line $cy$. After drawing the line segment $yz$ perpendicular to $cy$, move the lower end of the line segment to point $y$ as shown below.

In the example on the left, line $yz$ (shown in green) has been moved to the endpoint of line $cy$ (point $y$). It remains perpendicular to line $cy$.

Constrain this line by fixing it in position. Line $zy$ is fully constrained when it appears in black.
12.) Locate point b by offsetting lines 1,2 and 3,4 distances W and V respectively. Offset lines are shown in green.

Note: Some of the geometry is shown in blue as a means for making the visual information more clear.

13.) With point b as the center, draw a circle with radius F.
(Radius F = .1050 in this example)
The circle is shown in green.

Note: The circle should end up tangent to line zy. It may be necessary to force a tangent relationship in the event that rounding errors prevent that from happening.
14.) Locate the tooth tip by drawing a line (Shown in green) from the center of the pitch circle at an angle of $\frac{180^\circ}{N}$. In the example above, a 30 tooth sprocket yields an angle of $180/30 = 6$ degrees. The tooth tip is the intersection of the circle (center at b) and the line drawn from the center of the pitch circle, 6 degrees left of line 1,2.
15.) The tooth form NL, is outlined in red below. This represents ½ of the tooth form. The tooth form is comprised of 4 sections.

The images below illustrate the beginning of the trimming process necessary to reveal the tooth form.
16.) Continue the trimming process until only the tooth form and the (mirror axis) line 1,2 are remaining.

Make line 1,2 a construction line. Make the pitch circle a construction line. Refer to the illustration below.
17.) Mirror the tooth form about line 1,2. This represents an entire tooth form.

18.) Array this tooth form about the center of the pitch circle. Since there are 30 teeth on this example sprocket, array 30 instances of the tooth form, evenly spaced around the center of the pitch circle.
19.) Complete the sprocket drawing by extruding the sprocket to a measured thickness equal to that of the GEARS-IDS 30 tooth sprocket. *Note: Industry standard thickness = 0.93W – 0.006. The 0.006” represents a “clearance” number.*
20.) Create a 1” diameter hub with a 0.3” projection.

21.) Cut a 7/16” hex bore through the hub and sprocket. The hex is specified as the distance across two opposite flats. Create the hex by circumscribing it around a circle with a 7/16” diameter.
12.) Nylon or delrin sprockets need extra support to remain stiff and non deforming under load. The GEARS 30 tooth sprocket is cast with webbing as shown in figures 1 and 2 below. For added realism, measure the webbing on the GEARS-IDS sprocket with a dial caliper and create the sprocket geometry shown in the examples below.

*Note: For added realism, bevel the sprocket teeth as shown in figures 3 and 4 below. Other options include adding keyways and set screw or pin bores. For set screws refer to the GEARS drill and tapping lessons to learn how to specify hole sizes and thread pitch for various size screws.*

![Fig.2.) CAD Solid Model](image1)

![Fig.3.) Rendered Solid Model](image2)

![Fig.4.) 10 Tooth Solid Model w/ Bevel Tooth](image3)

![Fig.5.) 20 Tooth Solid Model w/ Bevel Tooth and 3/32” Keyway](image4)

Note: Use the GEARS-IDS spread sheet entitled *Equations for the Design of Standard Sprocket Teeth* to check the calculated values found using the equations listed in Table 1.